

Cambridge International Examinations

Cambridge Ordinary Level

CANDIDATE NAME			
CENTRE NUMBER		CANDIDATE NUMBER	
STATISTICS			4040/12
Paper 1		Oc	tober/November 2017
			2 hours 15 minutes
Candidates answer on	the Question Paper.		
Additional Materials:	Pair of compasses Protractor		

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions in Section A and not more than four questions from Section B.

If working is needed for any question it must be shown below that question.

The use of an electronic calculator is expected in this paper.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

This document consists of 17 printed pages and 3 blank pages.



Section A [36 marks]

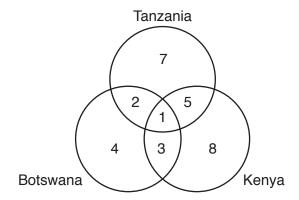
Answer all of the questions 1 to 6.

1	(a)	Sta	te, for each of the following, the name of a method of sampling in which	
		(i)	a sampling frame is never required,	
			[1]
		(ii)	every item in the population is numbered, and a random number table or generator is used to select every item in the sample,	S
			[1]
		(iii)	every item in the population is numbered, and a random number table or generator is used to select only the first item in the sample.	S
			[1]
	(b)	Cor	nsider the following statement, from which two statistical terms have been omitted.	
		ʻWh	en selecting a sample from a population, a researcher should, wherever possible, ensure	е
		tha	the sampling method is free from, and that the sample is	s
			of the population.'	
		Inse	ert the appropriate terms into the spaces to complete the statement.]

The	max	imum te	mpera	ature e	each w	eek ir	n a tov	vn was	s recoi	rded o	ver a	ten-week	period.		
(i)	The	followin	g valu	es, in	°C, ro	unded	d to the	e near	est int	eger,	were o	obtained.			
			23	24	22	26	28	23	28	32	29	28			
	For	these va	ılues,	find											
	(a)	the med	dian,												
										••••				[2]
	(b)	the mod	de,												
														[1]]
	(c)	the mea	an.												
														[2]
The	tem	perature	s in th	e tow	n were	origii	nally re	ecorde	ed corr	ect to	one d	lecimal pl	ace.		
ii)	Usir part	•	iginal	values	s, it mi	ght ha	ve be	en imp	ossib	le to fi	nd one	e of the m	easures	named ir	1
	Stat	te which	meas	ure, e	xplain	ing the	e reas	on for	your c	hoice					
														[1]]

2

3 A holiday company organises safari tours to African countries. The diagram below shows the number of the company's guides who have taken tours to one or more of the countries Tanzania, Botswana and Kenya.



Use this information to find the number of guides who have taken tours to

(i)	Botswana,
	[1]
(ii)	Tanzania and Kenya but not Botswana,
	[1]
(iii)	Tanzania or Kenya or both.
	[0]
	[2]
	the guides who have taken tours to Botswana, but only these guides, have also taken tours to babwe.
	the four countries Tanzania, Botswana, Kenya and Zimbabwe, find the number of guides who re taken tours to
(iv)	exactly two countries,
	[1]
(v)	at least three countries.
	[1]

4 A dental surgery is open for six days each week, and holds appointments each day in three sessions: morning, afternoon, and evening.

The table below shows measures for the number of appointments held in each session during one particular week.

Session	Mean	Standard deviation
Morning	6.33	0.745
Afternoon	5.33	2.810
Evening	2.50	1.260

				I .	i e e e e e e e e e e e e e e e e e e e
		Evening	2.50	1.260	
(i)		or which one of the nents was generally	sessions morning,	afternoon or evening	y, the number of
	(a) large	est,			
					[1]
	(b) mos	t varied.			
					[1]
(ii)	Find the	total number of appoir	ntments held in the su	rgery during this week	
					[2]
Fac	ch afternoc	on session lasts 4 hou	re		[<i>Z</i>]
Luc	on anomoc	n coodion acto i nou	10.		
(iii)	length of			y throughout the sess ge, during this particula	
					[2]

5 The table below summarises the performance of a hockey team for every match played in one season. For each match there are two pieces of information: the number of goals scored and the number of goals conceded.

				Number of g	goals scored	1	
		0	1	2	3	4	5 or more
	0	0	0	0	0	0	0
	1	1	1	0	1	0	2
Number	2	0	0	1	0	3	0
of goals conceded	3	0	1	1	4	2	2
	4	0	0	2	1	0	0
	5 or more	0	0	0	0	0	0

For example, there were three matches in which the team scored 4 goals and conceded 2 goals.

		• •	· ·
(i)	Fine	d the number of matches in which the team	
	(a)	conceded exactly 3 goals,	
			[1]
	(b)	scored 4 goals or more,	
			[1]
	(c)	scored the same number of goals as it conceded.	
			[1]
(ii)	Cal	culate the total number of goals conceded by the tea	m in the season.
			[2]
(iii)	Fxr	plain why it is not possible to calculate, from the tab	-
(,	-	red by the team in the season.	no abovo, the total hambor of goalo
			[1]

6	ess reco	ay, v ords,	ates who enter for a proficiency certificate with an examinate with specified minimum and maximum word limits, in the board knows that, for any subject, 3% of the essay rlength, and the remainder are of the specified length.	their subject of study. From its
	(i)		manager at the board selects at random an essay submitted in Sociology.	bmitted in History and an essay
		Fine	nd the probability that	
		(a)	both essays are of the specified length,	
				[2]
		(b)	the essay in History is of the specified length, but the e	essay in Sociology is not,
		(5)		[2]
		(c)	one of the essays is underlength and the other essay is	s overlengtn.
				[2]
	(ii)	In o	one particular year, 134 candidates submitted an essay th	nat was not of the specified length.
		Fine	nd the total number of essays submitted in that year.	
				[2]

Section B [64 marks]

Answer not more than **four** of the questions 7 to 11.

Each question in this section carries 16 marks.

7 In this question all pass rates, whether given or to be found, are expressed, or are to be expressed, as percentages.

At Lernalott School the academic ability of all enrolled A Level pupils, based on O Level performance, is recorded as one of outstanding, very good, good or modest.

The table below gives information on the number of enrolments and the pass rate in A Level Biology at the school, together with the standard population of enrolments for all A Level subjects at the school.

Academic ability group	Number of enrolments	Ability group pass rate (%)	Standard population of enrolments (%)
Outstanding	6	100.0	20
Very good	8	87.5	40
Good	5	80.0	30
Modest	4	50.0	10

For A Level Biology, calculate

III LITE STATIONAL DASS TAR	(i)	the stand	ardised	pass	rate
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(ii)	the crude pass rate.		 	[4]

.....[5]

The table below gives information on pass rates, over the same period of time, for pupils in other A Level subjects at Lernalott School.

Subject	Number of enrolments	Standardised pass rate (%)	Crude pass rate (%)
Chemistry	28	84.7	85.7
Physics	18	75.0	72.2
Chinese	25	73.3	80.0
Japanese	12	88.0	66.7
English	17	65.0	76.5

(iii)	State, with a reason, in which of these five subjects the highest quality of teaching appears to have been provided.
	[2]
(iv)	State in which of these five subjects the highest number of passes was obtained. Explain how this can be known without further calculation.
	[2]
	ublicity material the school gives crude pass rates for Arts, Sciences, Languages etc. (rather for individual subjects).
(v)	Calculate the crude pass rate for the languages Chinese, Japanese and English combined.
	[3]

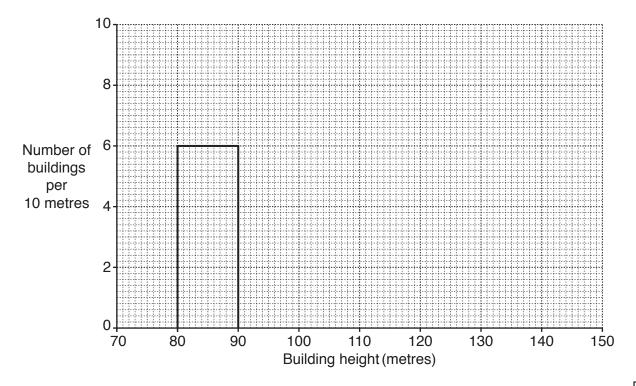
8 The following table summarises the heights of the 25 tallest buildings in a city.

Building height (metres)	Number of buildings	
80 – under 90	6	
90 – under 95	3	
95 – under 100	4	
100 – under 120	7	
120 – under 145	5	

(i) Estimate the mean height of these buildings.

[3]
 . [U]

(ii) On the following grid, draw a histogram to illustrate the data in the table above. The rectangle representing the 80 – under 90 class has already been drawn for you.

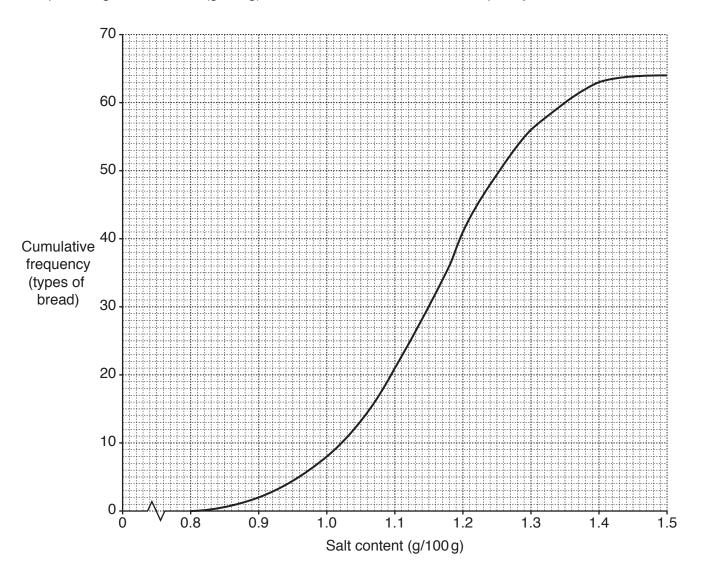


[4]

In the city a new building is being constructed which will have a height of 165 metres after

cor	npletion.	
(iii)	Estimate the new mean height of the 25 tallest buildings building.	in the city after the completion of this
		[2]
	e of the buildings has 20 floors (levels) of three different ty pors have only offices, and the remainder have only aparti	pes: 4 floors have only shops,
Thr	ee of the 20 floors are selected at random for routine safe	ty checks.
Fin	d the probability that	
(iv)	all three floors have apartments,	
		[2]
(v)	two floors have shops and one floor has offices,	
		[3]
(vi)	the floors are of different types.	
()	71	
		[2]

9 A particular supermarket sells 64 different types of bread. The salt content of these types, in grams per 100 grams of bread (g/100 g), is illustrated in the cumulative frequency curve below.



- (i) Use the graph to estimate, for these types of bread,
 - (a) the median salt content,

......g/100g [1]

(b) the interquartile range of the salt content,

......g/100g [4]

(c) the value of p, if the pth percentile of the salt content is 1.35 g/100 g.

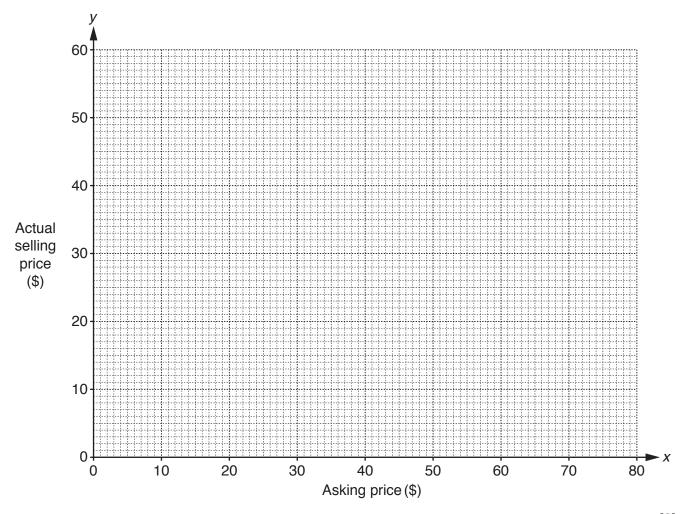
.....[2]

For	a he	althy diet, the government recommends a maximum salt content for bread of 1.0 g/100 g.
(ii)	Use	the graph to estimate, for these types of bread,
	(a)	the number which meet the government's recommendation,
		[1]
	(b)	the median salt content of those which do not meet the government's recommendation.
		g/100g [2]
٨ ٥	iovori	
_	dom.	nment food inspector, visiting this supermarket, selects four different types of bread at
Fin	d the	probability that she finds
(iii)	non	e which meet the government's recommendation,
		[3]
(iv)	at le	east one which meets the government's recommendation.
		[2]
Late	er, th	e supermarket reduces the salt content of all types of bread by 0.05 g/100 g.
(v)	Sta	te, explaining your answer, which of the measures found in part (i) will be unchanged. You
	are	not required to recalculate the measures.
		[1]

10 Pedro is a market trader who displays no prices on the items he offers for sale. When a potential customer shows interest in an item, Pedro states his asking price. Usually, following bargaining, if he sells the item it will be for a different price. His daughter Manuela (a statistics student) observes eight transactions her father makes, and in each case records the asking price and the actual selling price. Her results are shown in the following table.

Item	Α	В	С	D	Е	F	G	Н
Asking price, x (\$)	15	35	40	75	10	65	60	25
Actual selling price, y (\$)	12	20	40	55	8	45	35	20

(i) Plot these data on the grid below.



The data have an overall mean of (40.625, 29.375) and an upper semi-average of (60, 43.75).

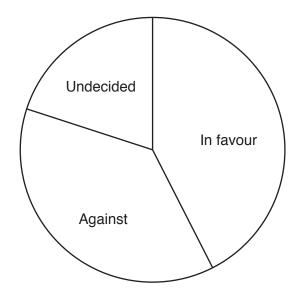
(ii)	Find the lower semi-average, and plot this and the two given averages on your graph.
(iii)	Use your plotted averages to draw a line of best fit, and find its equation in the form $y = mx + c$.
	[4
(iv)	Use your line to estimate, to the nearest \$5, for other transactions,
	(a) the actual selling price of an item with an asking price of \$55,
	(b) the asking price for an item which Pedro wishes to sell for \$50.
	[2
	nuela observes from her line of best fit that, overall, Pedro's actual selling price is proximately $k\%$ less than the asking price.
(v)	Use your answer to part (iii) to estimate the value of k.
(vi)	State, with a reason, for which of the items A – H Pedro will be most satisfied with the business
(**/	transacted.

										10								
11	A restaurant mar the use of mobile																	s on a proposed ban or gram below.
		B																\$
	Males	9	7	7	7	7	7	7	7	7	7	7	7	\$	7	\$		
		?	?	?	?	?	?	?	?									
	Females	7	7	7	7	7	7	7	7									
		?	?	?	?	?	?											
	= 1 person in For this sample,	favo	ur o	fa∣	ban		\$ =	= 1	pers	son	aga	iinst	ab	oan		? =	: 1 p	person undecided
	(i) state the tot	al nu	ımb	er c	of CL	ısto	mer	'S W	ho '	wer	e in	fav	our	of a	a ba	n,		
	(ii) state how m	nany	few	er f	ema	ales	we	re a	ıgai	nst	a ba	an tl	han	in f	favo	ur c	of it,	[1] , [1]
	(iii) calculate the	e pei	rcer	ntag	e of	all	the	cus	ston	ners	wh	o ha	ad a	a de	ecid	ed c	pin	ion on the ban.

The results shown in the pictogram are to be represented in comparative pie charts drawn to scale; one for males and one for females. The chart for males has already been drawn for you on the opposite page.

(iv) Draw, on the opposite page, the chart for females.

[5]



(v)	Ву	comparing the pie charts, write down three conclusions that may be drawn from the survey.
	1	
	2	
	3	[3]
(vi)	For	survey results, give one advantage of
	(a)	a pictogram presentation over a pie chart presentation,
		[1]
	(b)	a pie chart presentation over a pictogram presentation.
		[1]
In c	ondu	ucting a survey, open or closed questions may be used.
(vii)		te, for the restaurant manager's survey, which of these types of question she seems to e used. Explain your answer.
		[1]

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